

## Chp.5: Polynomial Functions

polynomial function: expression with coefficients and variables

Linear (degree of 1)  
 $ax + b$

ex)  $2x + 4$   
↑  
Leading coefficient

Quadratic (degree of 2)

$$ax^2 + bx + c$$

ex)  $-x^2 + 5x + 3$   
↑  
Leading coefficient = -1

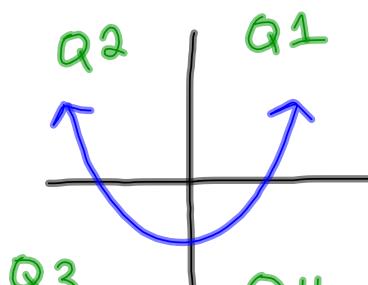
Cubic (degree of 3)

$$ax^3 + bx^2 + cx + d$$

ex)  $4x^3 - 6$

## End behavior

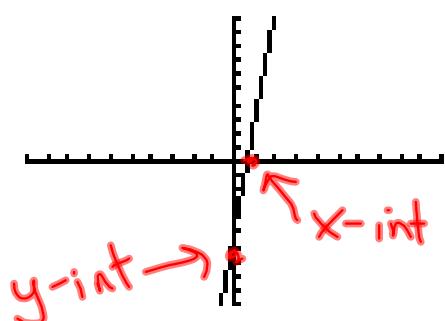
Where the ends of a graph extends.



extends up in  
Quadrants 1 + 2.

Linear

$$y = 8x - 5$$



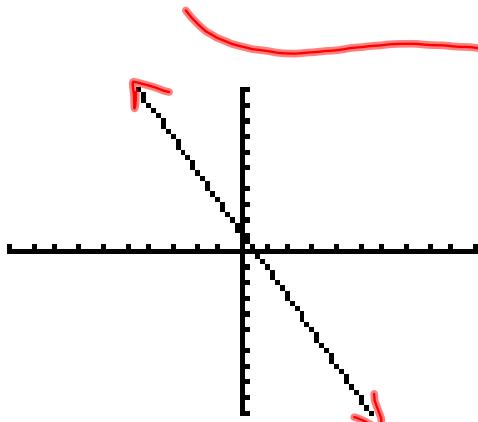
positive leading coefficient

End behavior

Extends up in Q1  
Down in Q3.

- no turning point

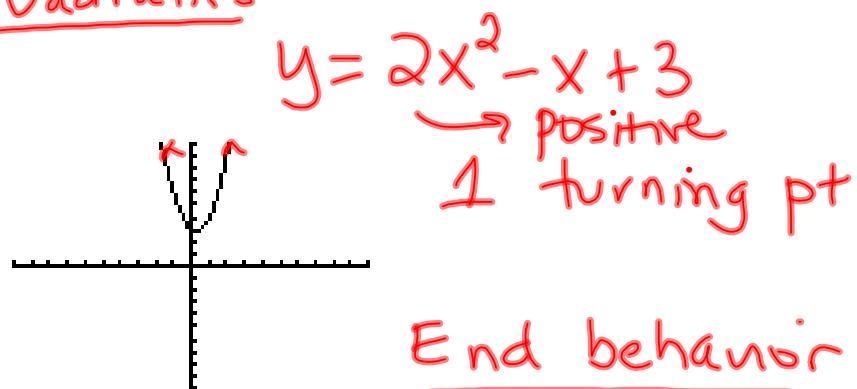
$$y = -2x + 1$$



negative

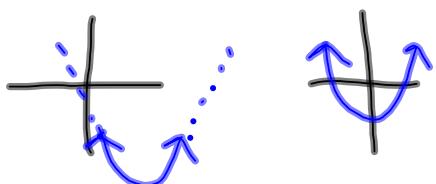
End behavior

extends up in Q2  
down in Q4

QuadraticsEnd behavior

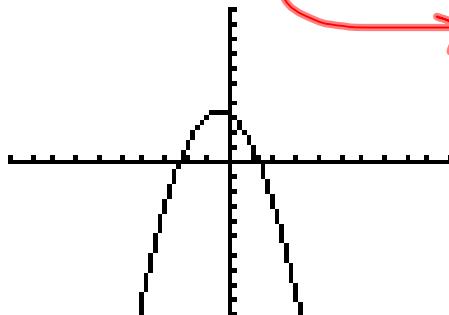
Extends up in Q1 & Q2

\* All positive quadratics extend up in Q1 & Q2.  
 exs)



$$y = -x^2 - x + 3$$

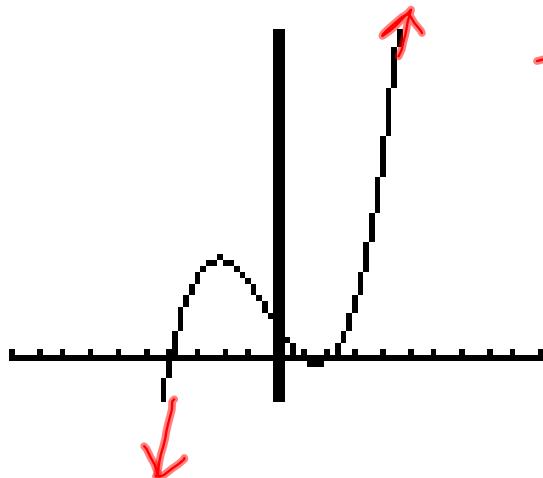
→ negative

End behavior

Extends down  
in Q3 & Q4

Cubic

$$x^3 + x^2 - 10x + 8$$



- positive
- two turning points

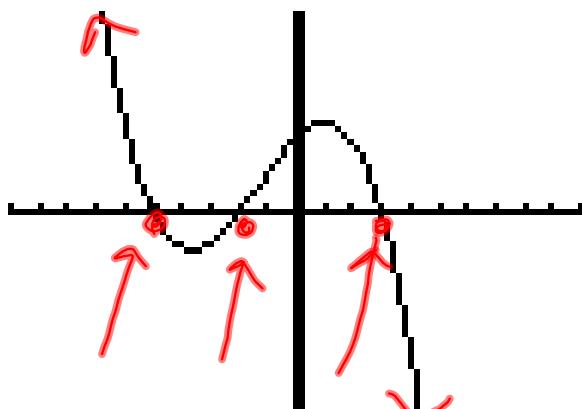
End Behavior

Extends up in Q1  
& down in Q3

$$y = -(x-3)(x+2)(x+5)$$

$$-x^3$$

- negative leading coefficient



- two turning pts

3-x intercepts

EB: extends up  
Q2 & down  
in Q4

## Domain & Range

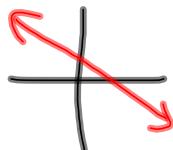
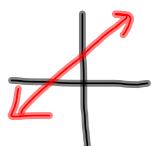
Domain: all x-values

→ where the graph extends  
left → right.

Range: all y-values

→ where the graph extends  
up & down.

### Linear

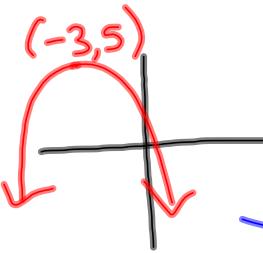
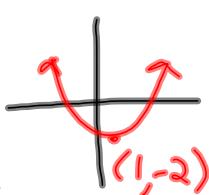


$$D: x \in \mathbb{R}$$

$$R: y \in \mathbb{R}$$

\* no restriction  
ALWAYS!

### Quadratics



$$D: x \in \mathbb{R} \text{ (Always!)}$$

\* Range Changes!

$$R: \{y | y \geq -2, y \in \mathbb{R}\}$$

$$R: \{y | y \leq 5, y \in \mathbb{R}\}$$