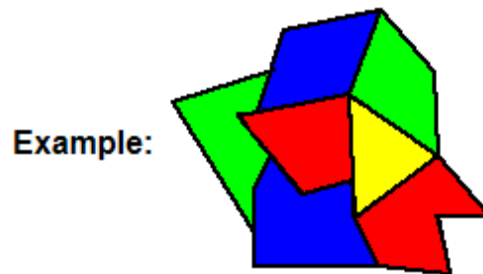


What are tessellations?

Basically, a tessellation is a way to tile a floor (that goes on forever) with shapes so that there is no overlapping and no gaps. Remember the last puzzle you put together? Well, that was a tessellation! The shapes were just really weird.

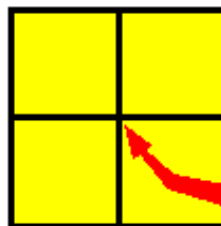


We usually add a few more rules to make things interesting!

REGULAR TESSELLATIONS:

- RULE #1: The tessellation must tile a floor (that goes on forever) with no overlapping or gaps.
- RULE #2: The tiles must be regular polygons - and all the same.
- RULE #3: Each *vertex* must look the same.

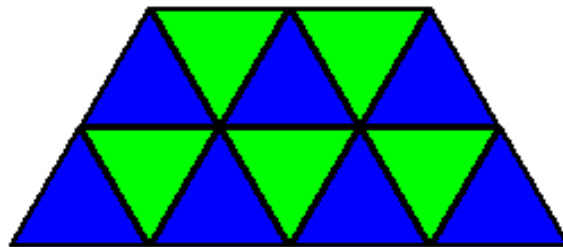
What's a vertex?



where all the "corners" meet!

What can we tessellate using these rules?

Triangles? Yep!

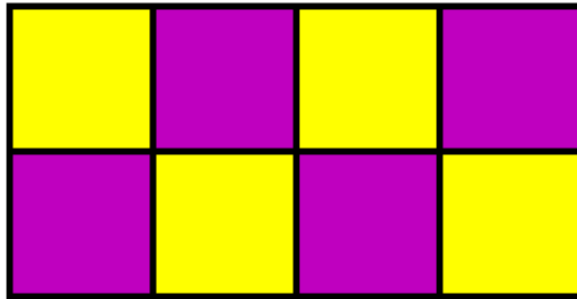


Notice what happens at each vertex!

The interior angle of each equilateral triangle is
60 degrees.....

$$60 + 60 + 60 + 60 + 60 + 60 = 360 \text{ degrees}$$

Squares? Yep!



What happens at each vertex?

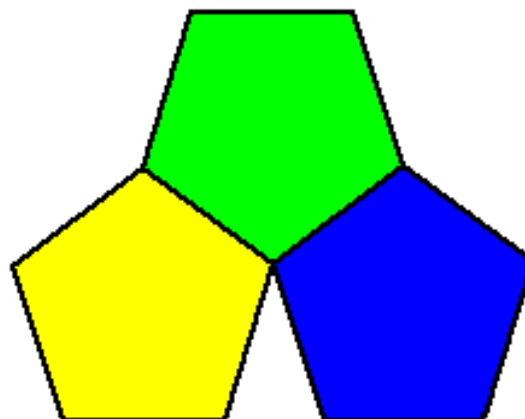
$$90 + 90 + 90 + 90 = 360 \text{ degrees again!}$$

So, we need to use regular polygons that add up to 360 degrees.

Will pentagons work?

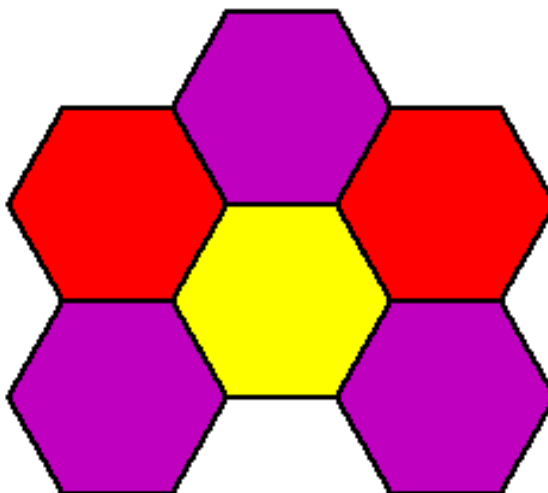
The interior angle of a pentagon is 108 degrees. . .

$108 + 108 + 108 = 324$ degrees . . . Nope!



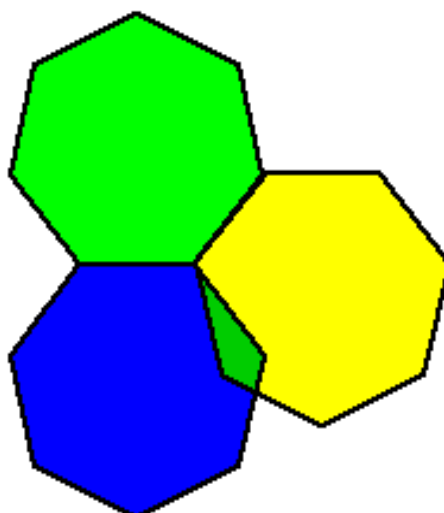
Hexagons?

$$120 + 120 + 120 = 360 \text{ degrees Yep!}$$



Heptagons?

No way!! Now we are getting overlaps!



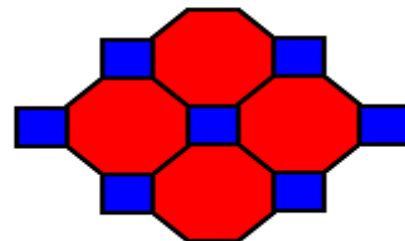
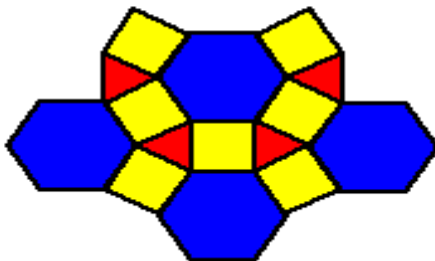
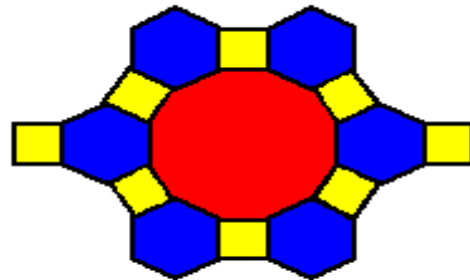
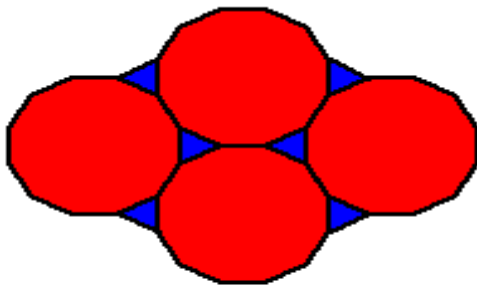
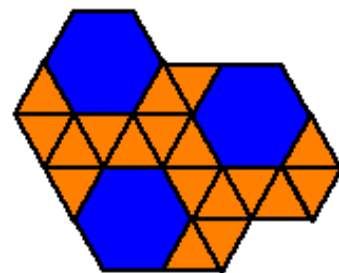
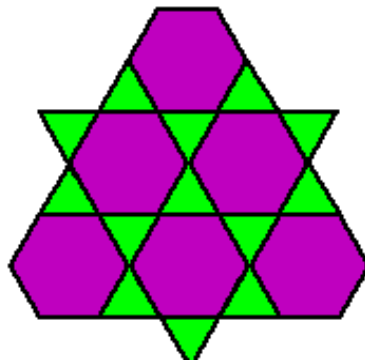
Octagons? Nope!

**They'll overlap too. In fact, all polygons with more than six sides will overlap!
So, the only regular polygons that tessellate are triangles, squares and
hexagons!**

SEMI-REGULAR TESSELLATIONS:


These tessellations are made by using two or more different regular polygons. The rules are still the same. Every vertex must have the exact same configuration.

Examples:



How is the pattern in a soccer ball a tessellation?



 <http://www.coolmath4kids.com/tesspag1.html>