## DO NOT OPEN THIS EXAMINATION PAPER UNTIL YOU ARE TOLD BY THE SUPERVISOR TO BEGIN

Mathematics 1201
Final Examination
June, 2018
Student Name: $\qquad$
Teacher Name: $\qquad$
Total Value: 70 marks
Time: 2 Hours

## general instructions

1. Candidates are required to do all items.
2. The examination has a total of 18 pages (including this cover) consisting of the following parts:

| Part I: | 35 Selected Response Items | Value: 35 marks |
| :--- | :--- | :--- |
| Part II: | 12 Constructed Response Questions | Value: |
| 35 marks |  |  |

3. Page 16 is a formulae sheet to be used for the exam. This page may be removed.
4. Part I should be completed on the answer sheet (Page 17). This page may be removed.
5. Answers to the constructed response questions for Part II are to be placed on this paper in the spaces provided.
6. For Part II items, candidates are reminded to show ALL necessary steps and calculations. Partial credit may be awarded for logical work even though you might not arrive at the correct solution. Correct answers without appropriate calculations will not merit full marks.
7. A self-powered calculator may be used for calculations and to obtain special values. Graphing calculators are to be reset before the examination begins.

## REGULATIONS FOR CANDIDATES

Candidates are expected to be thoroughly familiar with all regulations pertaining to their conduct during examinations. Candidates must comply with all requirements governing the following matters.

- Materials required
- Leaving the room
- Materials not permitted
- Models of calculators permitted
- Use of pen or pencil
- Use of unauthorized means and penalties
- Completion of required information
- Communication during the exam


## Part I

## Total Value: 35 Marks

1. Which would you use as a referent for an inch?
A) length of your foot
B) thickness of a dime
C) width of your thumb
D) your arm span
2. What is 9 yards (yd.) to the nearest centimetre (cm)?
A) 91
B) 128
C) 324
D) 823
3. A soccer ball has a radius of 11 cm . What is the surface area of the soccer ball in $\mathrm{cm}^{2}$ ?
A) 276
B) 1520
C) 5572
D) 19088
4. What is the surface area of the right square pyramid to the nearest $\mathrm{cm}^{2}$ ?
A) 66
B) 84
C) 96
D) 156

5. A cone has a volume of 1465 cubic feet $\left(\mathrm{ft}^{3}\right)$. What is the radius to the nearest foot (ft)?
A) 6
B) 10
C) 50
D) 100

6. What is the surface area of a hemisphere with a radius of 4 cm , in $\mathrm{cm}^{2}$ ?
A) 75
B) 100
C) 151
D) 201


Page 2 of 17
7. What is $\sqrt[4]{162}$ in simplest radical form?
A) $2 \sqrt[4]{3}$
B) $3 \sqrt[4]{2}$
C) $9 \sqrt[4]{2}$
D) $2 \sqrt[4]{9}$
8. What is the least common multiple for 21 and 45 ?
A) 105
B) 210
C) 315
D) 945
9. Which is a rational number?
A) $\sqrt{16}$
B) $\sqrt{20}$
C) $\sqrt[3]{35}$
D) $\sqrt[3]{60}$
10.What is $2 \sqrt[3]{5}$ expressed as an entire radical?
A) $\sqrt[3]{7}$
B) $\sqrt[3]{10}$
C) $\sqrt[3]{20}$
D) $\sqrt[3]{40}$
11.Simplify: $\quad\left(a^{3} b^{4}\right)\left(a^{-2} b\right)$
A) $\frac{b^{4}}{a^{6}}$
B) $\frac{b^{4}}{a^{5}}$
C) $a^{5} b^{3}$
D) $a b^{5}$
12.Simplify: $\quad \frac{m^{6} n^{4}}{m^{3} n^{8}}$
A) $\frac{m^{2}}{n^{2}}$
B) $\frac{m^{3}}{n^{4}}$
C) $m^{3} n^{4}$
D) $m^{9} n^{12}$
13. Which is equivalent to $\left(\sqrt{\frac{3}{4}}\right)^{-3}$ ?
A) $\left(-\frac{4}{3}\right)^{\frac{3}{2}}$
B) $\left(-\frac{3}{4}\right)^{\frac{3}{2}}$
C) $\left(\frac{3}{4}\right)^{\frac{2}{3}}$
D) $\left(\frac{4}{3}\right)^{\frac{3}{2}}$
14. Expand: $\quad 2 x(3 x+1)$
A) $5 x^{2}+3 x$
B) $6 x+2$
C) $6 x^{2}+1$
D) $6 x^{2}+2 x$
15.What is the greatest common factor of $8 a^{2} b^{3}+4 a b$ ?
A) $2 a b$
B) $2 a^{2} b$
C) $4 a b$
D) $4 a^{2} b^{3}$
16. Expand and simplify $(3 x-2)(5 x+3)$
A) $15 x^{2}-x-6$
B) $15 x^{2}-x+6$
C) $15 x^{2}-4 x-6$
D) $15 x^{2}+19 x+6$
17. Factor: $\quad x^{2}-13 x+36$
A) $(x+3)(x+12)$
B) $(x-2)(x-18)$
C) $(x+6)(x-6)$
D) $(x-4)(x-9)$
18. Factor: $\quad 18 k^{2}-50$
A) $2(3 k-5)(3 k+5)$
B) $2(3 k-5)(3 k-5)$
C) $(9 k-25)(9 k+25)$
D) $(9 k-25)(9 k-25)$
19. Factor: $\quad 9 x^{2}-24 x+16$
A) $(3 x-4)(3 x-4)$
B) $(3 x-8)(3 x-8)$
C) $(3 x+4)(3 x+4)$
D) $(3 x+8)(3 x+8)$
20. Factor: $\quad 2 x^{2}-2 x-12$
A) $2(x-2)(x+3)$
B) $2(x-6)(x+1)$
C) $2(x+2)(x-3)$
D) $2(x+6)(x-1)$
21. Which diagram represents a function?
A)

B)

C)

D)

22. If $f(x)=2 x+1$ and $g(x)=3 x-2$, what is the value of $f(2) \times g(3)$ ?
A) 12
B) 13
C) 28
D) 35
23.What is the domain and range of the graph?
A) $\{x \mid-3 \leq x \leq 4, x \in \mathbb{R}\}$ $\{y \mid-5 \leq y \leq 2, y \in \mathbb{R}\}$
B) $\{x \mid-3<x \leq 4, x \in \mathbb{R}\}$ $\{y \mid-5 \leq y<2, y \in \mathbb{R}\}$
C) $\{x \mid-3<x<4, x \in \mathbb{R}\}$ $\{y \mid-5<y<2, y \in \mathbb{R}\}$

D) $\{x \mid-3 \leq x<4, x \in \mathbb{R}\}$ $\{y \mid-5<y \leq 2, y \in \mathbb{R}\}$
24. What is the equation of the line?
A) $y=-\frac{3}{2} x+6$
B) $y=-\frac{3}{2} x+4$
C) $y=\frac{3}{2} x+6$
D) $y=\frac{3}{2} x+4$

25. What is the equation of the line that passes through $(-1,4)$ with a slope of 5 ?
A) $(y-4)=5(x+1)$
B) $(y-1)=5(x+4)$
C) $(y-4)=5(x-1)$
D) $(y+1)=5(x-4)$
26. What is the slope of a line perpendicular to $y=-\frac{4}{3} x+2$ ?
A) $-\frac{4}{3}$
B) $-\frac{3}{4}$
C) $\frac{4}{3}$
D) $\frac{3}{4}$
27. What is the solution to the following system of equations?
A) $(-6,0)$
B) $(-3,1)$
C) $(0,-5)$
D) $(0,2)$

28. Declan has $\$ 2.50$ worth of nickels and dimes. If he has 36 coins in total, which system of linear equations models this situation?
A) $\left\{\begin{array}{c}n+d=2.50 \\ 0.05 n+0.10 d=36\end{array}\right.$
B) $\left\{\begin{array}{c}n+d=2.50 \\ 0.10 n+0.05 d=36\end{array}\right.$
C) $\left\{\begin{array}{r}n+d=36\end{array}\right.$
$\{0.05 n+0.10 d=2.50$
D) $\left\{\begin{array}{c}n+d=36 \\ 0.10 n+0.05 d=2.50\end{array}\right.$
29. What is the solution to the system of equations?

$$
\left\{\begin{array}{c}
2 x+5 y=6 \\
-2 x+3 y=10
\end{array}\right.
$$

A) $(-9,-2)$
B) $(-2,2)$
C) $(8,-2)$
D) $(4,6)$
30. Which linear system has an infinite number of solutions?
A) $\left\{\begin{array}{c}y=x+3 \\ -3 x+3 y=4\end{array}\right.$
B) $\left\{\begin{array}{l}8 x+2 y=6 \\ y=-4 x+3\end{array}\right.$
C) $\left\{\begin{array}{c}y=3 x \\ 5 x+y=0\end{array}\right.$
D) $\left\{\begin{array}{c}4 x+8 y=20 \\ y=2 x-15\end{array}\right.$
31. In $\triangle D E F$, which of the following is equal to $\frac{5}{13}$ ?
A) $\sin E$
B) $\sin D$
C) $\tan E$
D) $\tan D$

32. Which of the following trigonometric ratios can be used to find the length of $k$ ?
A) $\sin 40^{\circ}=\frac{12}{k}$
B) $\sin 40^{\circ}=\frac{k}{12}$
C) $\tan 40^{\circ}=\frac{18}{k}$
D) $\tan 40^{\circ}=\frac{k}{18}$

33. What is the measure of $\angle A$ ?
A) $30^{0}$
B) $35^{0}$
C) $55^{0}$
D) $60^{\circ}$

34. Jayne is standing 4.2 m from the base of a tree in her backyard. The angle of inclination from her line of sight to the top of the tree is $62^{\circ}$. If her eyes are 1.3 m above the ground, what is the height of the tree to the nearest tenth of a metre?
A) 3.7
B) 5.0
C) 9.2
D) 7.9

35.A car is observed at an angle of depression of $48^{0}$ from the top of a building. If the car is 55 m from the base of the building, how tall is the building?
A) 49.5 m
B) 61.1 m
C) 74.0 m
D) 82.2 m


## Part II

## Total Value: 35 Marks

Value
3
36. Tennis balls are sold 3 per package in a sealed cylindrical tube with a height of 8.5 inches. Each tennis ball has a diameter of 2.7 inches. Calculate the amount of empty space in the tube.

37. A) The surface area of a cube is $294 \mathrm{~cm}^{2}$. What is the volume of the cube in $\mathrm{cm}^{3}$ ?


Value
37. B) Simplify: $\frac{\left(3 x^{-1} y^{2}\right)^{2}\left(2 x^{2} y^{-1}\right)^{3}}{9 x^{2} y^{3}}$ contain only positive exponents

Value
38. C) Determine the simplified expression that would represent the area of the shaded region.
$(2 x-5)$

39. A) The function $C(n)=0.70 n+8$, represents the cost, C , in dollars, of downloading $n$ songs from an online music store.
i) Determine $C(46)$. What does this number represent?
ii) Determine the value of $n$ when $C(n)=67.50$. What does this number represent?
39. B) Sketch the graph that represents a car's speed given:

- It travels at $80 \mathrm{Km} / \mathrm{h}$ for 10 seconds.
- Over 5 seconds it slows down at a constant rate to $50 \mathrm{Km} / \mathrm{h}$.
- It travels at $50 \mathrm{Km} / \mathrm{h}$ for 15 seconds.
- It speeds up to $70 \mathrm{Km} / \mathrm{h}$ at a constant rate over 10 seconds.


40. A) A line passes through the points $(4,2)$ and $(-8,6)$. Determine the equation of the line in general form. $(A x+B y+C=0)$.

Value
3
40. B) Show that $\triangle A B C$ is a right triangle.


3 41. James is building towers using white and grey cubes. When he stacks 6 white cubes on 3 grey cubes, the tower is 7.5 feet high. When he stacks 2 white cubes on 5 grey cubes, the tower is 6.5 feet high. Write and algebraically solve a system of equations to determine $x$ and $y$ in inches.

$\qquad$ in.
$\qquad$ in.

Value

3
42. Find the area of the circle with centre 0 .


## Math 1201 Formulae Sheet

(This sheet may be removed from the exam paper.)

Measurement

| Imperial | Imperial to SI Units |
| :---: | :---: |
| $1 \mathrm{ft} .=12 \mathrm{in}$. | $1 \mathrm{in} .=2.54 \mathrm{~cm}$ |
| $1 \mathrm{yd} .=3 \mathrm{ft}$. | $1 \mathrm{mi} .=1.6 \mathrm{~km}$ |
| $1 \mathrm{mi} .=1760 \mathrm{yd}$. |  |

Surface Area and Volume

| Surface Area | Volume |
| :---: | :---: |
| Cylinder |  |
| $A=2 \pi r^{2}+2 \pi r h$ |  |
| $A=\pi r^{2}+\pi r s$ |  |
| Cone | Pyramid |
|  | $V=\frac{1}{3}[l \times w \times h]$ |
| Sphere |  |
| $A=4 \pi r^{2}$ | $V=\frac{1}{3}\left[\pi r^{2} h\right]$ |
|  |  |

Math 1201 Selected Response Answer Sheet
(This sheet may be removed from the exam paper.)
$\qquad$ Teacher Name: $\qquad$

| 1. | 11. | 21. | 31. |
| :---: | :---: | :---: | :---: |
| 2. $\qquad$ | $12 .$ | 22. | 32. |
| 3. | 13. | 23. | 33. |
| 4. | $14 .$ | 24. | 34. |
| 5. | 15. | $25 .$ | 35. |
| 6. | 16. | 26. |  |
| 7. | 17. | 27. |  |
| 8. | 18. | 28. |  |
| 9. | 19. | 29. |  |
| 10. | 20. | 30. |  |

